

P02: Transport properties of C-S-H

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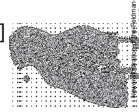
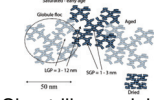
Project description

Moisture transport in cementitious materials is instrumental to understand their durability. Calcium silicate hydrate phases are the reaction product between cement and water.

- C-S-H contains the smallest pores being found in cement
- **There is no general agreement on the C-S-H structure**
- C-S-H may govern the moisture transport in cementitious materials if all other pores/cracks depercolate

Literature:

- Two major structural models are currently being discussed:
 - Colloidal models [Jennings2008]
 - Sheet-like models [FeldmanSereda1970]
- The material has a characteristic length scales of a few nano metres. Thus, the transport laws in such pores may deviate significantly from continuum values.
- Due to its amorphous character scattering data is hard to interpret
- There is no information about transport properties in just C-S-H.



Approach

- It is perceived that C-S-H's structure affects many of its properties in an ambiguous way. Thus, the connection of one structure with a given property is hard.
- By generating different model structures it is hoped to generate a clearer picture than just considering individual properties.

Project results – are perturbed sphere packings a good transport model for C-S-H?

Idea:

Particle models have been used to describe C-S-H. [Powers1958, Jennings2000, Ulm2012] Thus, the simplest imaginable particle model is used for C-S-H: monodisperse particles.

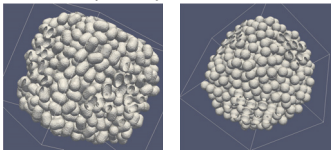
- Scattering results indicate a characteristic size of 4-5 nm for C-S-H particles [Skinner2010, Popova2002].
- NMR-results (McDonald) suggest porosities $\epsilon(\text{Gel})$ of 31 % and $\epsilon(\text{Sheet})$ of 24.5 %.

Hypothesis:

- Monodisperse particles suffice
- Continuum theory suffices.
- Gel pores are described as interparticle space
- Sheet pores are assumed to be contained within particles [Jennings2008] and are not modelled.

Approach

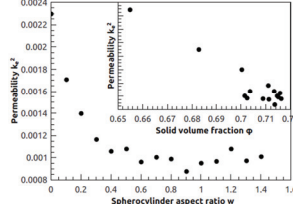
- Generate suitable packings with a suitable porosity.



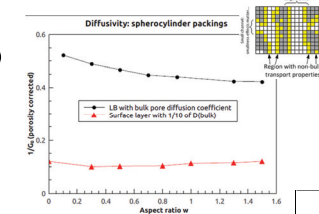
- Characterise their properties:
 - LB-Permeability: $v_0 = -\frac{k}{\mu}(\nabla p - g)$
 - LB-Diffusivity: $\frac{D}{D_0} = \frac{\epsilon \delta}{\tau^2} = \frac{\epsilon}{G}$
 - Compute the scattering pattern to compare against data available for C-S-H [Debye].

$$I(q) \propto \int_0^\infty \chi(r) r^2 \frac{\sin(qr)}{qr} dr$$

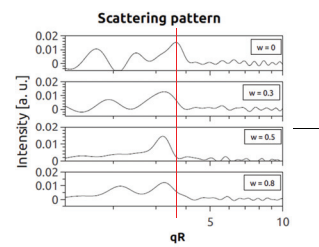
Permeability of spherocylinder packings



- Permeability for $\epsilon(\text{Gel}) = 31\%$. Minimum permeability for this model: $k = 4.5 \times 10^{-21} \text{ m}^2$



- Diffusion: $D(\text{bulk}) = 3 \times 10^{-10} \text{ m}^2/\text{s}$
 $D(\text{surf. L.}) = 7.4 \times 10^{-11} \text{ m}^2/\text{s}$



Transport data for "pure" C-S-H does not exist. However, this data may be approximated by data obtained for very mature and crack-free paste with depercolated pore systems. Thus, the lower limit of the literature data may be a base for comparison.

- Permeability: the lowest values in the literature go down to $10^{-23} \text{ m}^2/\text{s}$. [Cui2001]
- Diffusivity: the lowest values being found in the literature are $9.81 \times 10^{-12} - 6.3 \times 10^{-13} \text{ m}^2/\text{s}$ [Pigeon1998]
- The scattering curve obtained shows distinct peaks, in contrast to typical SANS results [Allen2007]

Conclusion

Monodisperse packings of spherical particles with continuum transport laws do not match the transport properties of C-S-H as estimated from experimental data.

The next step is to try different base units, e. g. (polydisperse) sheets (see below).

In principle, this approach can be applied to any perceivable structure.

Future plans

Investigation of other "simple model structures"

The idea is to use a random sequential addition (RSA) sequence to fill space with various geometric forms:

1. Determine insertion position and orientation.
2. Check whether insertion is possible w/o overlap

If no further insertion is possible, shrink inserted structure by some factor and return to 1. Repeat until space is filled to the desired level. This could be done with:

- Discs and similar platelets
- Spheres

Compute the resulting properties

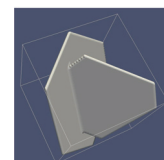
Study of 3D sheet growth structures

Synthetic C-S-H looks like clusters of sheets formed by homogenous nucleation. For C-S-H in cement paste, however, a heterogeneous nucleation growth mechanism is conceivable.

It is planned to investigate the formation and the properties of structures formed by interacting sheets.

- Straight sheets
- Crumpled sheets
- Sheets with "hard" interactions as well as attractive interactions

Key problem: how to represent a growing sheet in space?



Trials have been conducted for an approach based on a 3D cellular automaton with 2D oriented update sequence.

However, bent and randomly oriented sheets have not been realised

A finite element based vectorial description (triangles in space) has been considered. Different approaches are being currently evaluated.

Outstanding questions

- **Experimental data of the transport properties in C-S-H?** -> direct measurements on C-S-H would allow better conclusions.
- How to generate Feldman-Sereda type sheet structures?
- Modelling of mechanical properties of the structures?
- Obtaining a structure more consistent with all observations.

References

[1] Merlin M. Jennings. *Microstructure to solid model of c-s-h in cement*. Cui et al. *Cement and Concrete Research*, 36(2):272-284, 2006.
 [2] E. F. Faldutsky and P. J. Searles. *New model for hydrated pasted cement and its mechanical properties*. *Engineering Fracture Mechanics*, 173:103-116, 2017.
 [3] E. Faldutsky, E. R. Chou, C. J. Donkers, H. R. Wertz, and P. J. Searles. *Hydration of calcium silicate hydrate in cement*. *Physical Review Letters*, 118(12):125701, 2017.
 [4] G. F. Vignati. *Structure and physical properties of hydrated Portland cement paste*. *Journal of the American Ceramic Society*, 43(1):116-126, 1960.
 [5] Jian Zhou, Shuangshuang Li, Ruijun Zhu, and Abing Yu. *Direct random packings of spherocylinders*. *Soft Matter*, 8(2):202-212, 2012.
 [6] R. E. Munnich, R. L. Hill, and D. B. Peiffer. *Pore size and flow characteristics and permeability of cement*. *Polymer-Solvent Colloid*, Wiley, New York, 1962.
 [7] R. E. Munnich, R. L. Hill, and D. B. Peiffer. *Pore size and flow characteristics and permeability of cement*. *Polymer-Solvent Colloid*, Wiley, New York, 1962.
 [8] R. E. Munnich, R. L. Hill, and D. B. Peiffer. *Pore size and flow characteristics and permeability of cement*. *Polymer-Solvent Colloid*, Wiley, New York, 1962.
 [9] P. Cifre and A. M. Sanchez. *Scattering by an inhomogeneous solid*. *Journal of Applied Physics*, 20(2):103-110, 1949.
 [10] E. M. Ginter. *A proposed mechanism for the growth of c-s-h during the hydration of trisubstituted calcium silicate*. *Cement and Concrete Research*, 27:683-693, 1997.
 [11] P. F. James, C. J. Donkers, E. M. Ginter, and A. J. Van Duyn. *Direct random packings of spherocylinders*. *Journal of Applied Physics*, 95(10):5450-5453, 2004.
 [12] Cui and J. H. Chou. *Permeability and pore structure of c-s-h*. *Cement and Concrete Research*, 31:207-216, 2001.
 [13] J. H. Chou, J. H. Chou, and J. H. Chou. *Microstructure and Transport*. Springer Science + Business Media, New York, 2002.
 [14] American Ceramic Society. *Handbook of Ceramics*. American Ceramic Society, 1976.
 [15] J. H. Chou. *Characterization of c-s-h measured by its permeability*. *The Journal of Applied Physics*, 71(11):4919-4923, 1992.
 [16] J. H. Chou. *Characterization of c-s-h measured by its permeability*. *The Journal of Applied Physics*, 71(11):4919-4923, 1992.
 [17] J. H. Chou. *Characterization of c-s-h measured by its permeability*. *The Journal of Applied Physics*, 71(11):4919-4923, 1992.
 [18] R. D. Mindes. *Characterization of c-s-h measured by its permeability*. *The Journal of Applied Physics*, 71(11):4919-4923, 1992.
 [19] R. D. Mindes. *Characterization of c-s-h measured by its permeability*. *The Journal of Applied Physics*, 71(11):4919-4923, 1992.